Math 432: Set Theory and Topology HOMEWORK 4 Due date: Feb 23 (Thu)

Exercises from "A quick introduction to basic set theory". 2, 3, 4, 5

Other (mandatory) exercises.

- 1. Below, for the questions asking for examples, make sure your examples are different from those in the notes ("A quick introduction to basic set theory").
  - (a) Write down the ordinal 5 (the 6<sup>th</sup> least ordinal) explicitly.
  - (b) Give examples A, B of transitive sets such that the relation  $\in$  on A is not an ordering, but on B it is.
  - (c) Give an example of a non-transitive set.
- **2.** Recall that a function  $f : X \to Y$  is a *subset* of  $X \times Y$  satisfying a certain property. Give two different proofs that  $\{f(x) : x \in X\}$  is a set: one using only the Replacement axiom and one using only the Comprehension axiom.